

Zero Rate Return Indices (ZRR Indices)

The ZRR Index is a measurement of the total return from a synthetic portfolio investing in a constant maturity security. The constant maturity securities are derived from the ThaiBDC's *zero coupon yield curve*. The curve which relates the yield on a security to its time to maturity, is based on the quoted bidding yields on government bond and treasury bills by primary dealers. The index base date is **January 02, 2002** and all ZRR indices are set to **100**.

Eight ZRR indices currently available include:

- 1 month ZRR index
- 3 month ZRR index
- 6 month ZRR index
- 1 year ZRR index
- 2 year ZRR index
- 3 year ZRR index
- 4 year ZRR index
- 5 year ZRR index

1 day total return for holding 1 year constant maturity security = (Price of Synthetic T-Bill sold today) / (Price of Synthetic T-Bill bought today)
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$1\text{yrZRR } d1 = 100$ $1\text{yrZRR } d2 = 1\text{yrZRR } d1 * [(1 + ZR_{d1}(365/365))^{(365/365)}] / [(1 + ZR_{d2} ((365-\Delta d)/365))^{((365-\Delta d)/365)}]$ $1\text{yrZRR } d_n = 1\text{yrZRR } d_{n-1} * [(1 + ZR_{d(n-1)}(365/365))^{(365/365)}] / [(1 + ZR_{d(n)} ((365-\Delta d)/365))^{((365-\Delta d)/365)}]$
Where $d_n = \text{day } n$ $ZR_{\text{day}(n)}(\text{TTM}) = \text{Zero Yield Rate at TTM on Day } n$ $\Delta d = \text{number of day from previous working day to current day}$

Calculation Example of 1 year ZRR index calculation

January 02, 2002

$$1\text{yrZRR} = 100$$

January 03, 2002

$$\begin{aligned} \text{Price of 1 year (365 day) synthetic T-Bill (bought on Jan 02,2002)} \\ &= \text{par} / (1 + 1\text{yr Zero Yield}/100)^{(365/365)} \\ &= \text{par} / (1.024857654)^1 \end{aligned}$$

$$\begin{aligned} \text{Price of 364 day synthetic T-Bill (to be sold today)} \\ &= \text{par} / (1 + 364\text{day Zero Yield}/100)^{(364/365)} \\ &= \text{par} / (1.024770939)^{(364/365)} \end{aligned}$$

$$\begin{aligned} \text{Return on 1 day holding 1yr T-Bill} \\ &= \text{Price of Synthetic T-Bill sold today} / \text{Price of Synthetic T-Bill bought today} \\ &= [\text{par} / (1 + 364\text{day Zero Yield}/100)^{(364/365)}] / [\text{par} / (1 + 1\text{yr Zero Yield}/100)^1] \\ &= [(1.024857654)^1] / [(1.024770939)^{(364/365)}] \end{aligned}$$

$$\begin{aligned} 1\text{yrZRR} &= 100 * \text{Return on 1 day holding 1yr T-Bill} \\ &= 100 * [(1.024857654)^1] / [(1.024770939)^{(364/365)}] \\ &= \underline{100.0151665} \end{aligned}$$

January 04, 2002

$$\begin{aligned} \text{Price of 1 year (365 day) synthetic T-Bill (bought on Jan 03,2002)} \\ &= \text{par} / (1 + 1\text{yr Zero Yield}/100)^{(365/365)} \\ &= \text{par} / (1.02477547469)^1 \end{aligned}$$

$$\begin{aligned} \text{Price of 364 day synthetic T-Bill (to be sold today)} \\ &= \text{par} / (1 + 364\text{day Zero Yield}/100)^{(364/365)} \\ &= \text{par} / (1.02491519097)^{(364/365)} \end{aligned}$$

$$\begin{aligned} \text{Return on 1 day holding 1yr T-Bill} \\ &= \text{Price of Synthetic T-Bill sold today} / \text{Price of Synthetic T-Bill bought today} \\ &= [\text{par} / (1 + 364\text{day Zero Yield}/100)^{(364/365)}] / [\text{par} / (1 + 1\text{yr Zero Yield}/100)^1] \\ &= [(1.02477547469)^1] / [(1.02491519097)^{(364/365)}] \end{aligned}$$

$$\begin{aligned} 1\text{yrZRR} &= 100.0151665 * \text{Return on 1 day holding 1yr T-Bill} \\ &= 100.0151665 * [(1.02477547469)^1] / [(1.02491519097)^{(364/365)}] \\ &= \underline{100.0082752} \end{aligned}$$

January 07, 2002

$$\begin{aligned} \text{Price of 1 year (365 day) synthetic T-Bill (bought on Jan 04,2002)} \\ &= \text{par} / (1 + 1\text{yr Zero Yield}/100)^{(365/365)} \\ &= \text{par} / (1.0249189205)^1 \end{aligned}$$

$$\begin{aligned} \text{Price of 362 day synthetic T-Bill (to be sold today)} \\ &= \text{par} / (1 + 362\text{day Zero Yield}/100)^{(362/365)} \\ &= \text{par} / (1.02480274745)^{(362/365)} \end{aligned}$$

$$\begin{aligned} \text{Return on 3 day holding 1yr T-Bill} \\ &= \text{Price of Synthetic T-Bill sold today} / \text{Price of Synthetic T-Bill bought today} \\ &= [\text{par} / (1 + 362\text{day Zero Yield}/100)^{(362/365)}] / [\text{par} / (1 + 1\text{yr Zero Yield}/100)^1] \\ &= [(1.0249189205)^1] / [(1.02480274745)^{(362/365)}] \end{aligned}$$

$$\begin{aligned} 1\text{yrZRR} &= 100.0082752 * \text{Return on 3 day holding 1yr T-Bill} \\ &= 100.0082752 * [(1.0249189205)^1] / [(1.02480274745)^{(362/365)}] \\ &= \underline{100.0397554} \end{aligned}$$